

## The Quadratic Formula

Using the **quadratic formula**, we can solve all quadratic equations.

$$\text{If } ax^2 + bx + c = 0, \text{ then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Solve the equations  $6x - 1 = x^2$

First, we put the equation in **standard form** by subtracting  $6x$  and adding  $1$  to both sides. Re-write in descending order:

$$x^2 - 6x + 1 = 0$$

$$a^2 + b^2 = c^2 \text{ (standard form of a quadratic equation)}$$

$$\text{using this we see that } a = 1, b = -6 \text{ and } c = 1$$

Next, we substitute these values into the quadratic formula and then begin to simplify.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-(-6) \pm \sqrt{b(-6)^2 - 4(1)(1)}}{2(1)}$$

Substitute  $a = 1, b = -6, c = 1$  into the formula. Place the parentheses on the numbers to avoid making mistakes on “signs”  
Simplify.

$$x = \frac{6 \pm \sqrt{36 - 4}}{2}$$

Note: the fact that  $b^2 - 4ac$  is not equal to a perfect square indicates that it is not possible to solve this equation by factoring.

$$x = \frac{6 \pm \sqrt{32}}{2}$$

Next, we need to simplify the radical:  $\sqrt{32} = \sqrt{16}\sqrt{2}$ ;

$$\text{which give us: } 4\sqrt{2}$$

$$x = \frac{6}{2} \pm \frac{4\sqrt{2}}{2}$$

then we simplify

$$x = 3 \pm 2\sqrt{2}$$

thus, our two solutions:  $3 + 2\sqrt{2}, 3 - 2\sqrt{2}$

**Exercises: Solve the equations using quadratic formula.**

1.  $x^2 + 2x - 24 = 0$

2.  $2x(x - 3) = 2$

3.  $\frac{1}{2}x^2 + \frac{3}{2}x - 2 = 0$

4.  $7x^2 + 4 = 2x$

**Answers:**

1. {4, 6}      2.  $\left\{\frac{3 \pm \sqrt{13}}{2}\right\}$       3. {-4, 1}      4.  $\left\{\frac{1 \pm 3i\sqrt{3}}{7}\right\}$