

Statistics formulas for STA 2023 and STA 2122

Z-Score for Sample Values and Population Values

| | |
|-----------------------------|------------------------------|
| $Z = \frac{x - \bar{x}}{s}$ | $Z = \frac{X - \mu}{\sigma}$ |
|-----------------------------|------------------------------|

Standard Deviation for Sample Values and Population Values

| | |
|---|--|
| Sample Standard Deviation, $s = \sqrt{\frac{\sum(x - \bar{x})^2}{n - 1}}$ | Population Standard Deviation, $\sigma = \sqrt{\frac{\sum(x - \mu)^2}{N}}$ |
|---|--|

Sampling Distribution for a Sample Proportion

| | | | |
|---|---------------------|--|---|
| $\hat{p} = \frac{x}{n}$ | $\mu_{\hat{p}} = p$ | $\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$ | $Z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}}$ |
| Central Limit Theorem Conditions ($\hat{p} \sim normal$) | 1. SRS | 2. $np \geq 10$; and $n(1-p) \geq 10$ | 3. $N \geq 10n$ |

Sampling Distribution for a Sample Mean

| | | | |
|--|-----------------------|--|---|
| $\bar{x} = \frac{\sum x}{n}$ | $\mu_{\bar{x}} = \mu$ | $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$ | $Z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$ |
| Central Limit Theorem Conditions ($\bar{x} \sim normal$) | 1. SRS | 2. $n \geq 30$ or $x \sim normal$ | |

Confidence Intervals and Test Statistics for Hypothesis Testing

| CI for μ , σ known | CI for μ , σ unknown | CI for p |
|---|--|--|
| C.I. = $\bar{x} \pm Z \frac{\sigma}{\sqrt{n}}$ | C.I. = $\bar{x} \pm t \frac{s}{\sqrt{n}}$ | C.I. = $\hat{p} \pm Z_c \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$ |
| HT for μ , σ known | HT for μ , σ unknown | HT for p |
| $Z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$ | $t = \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n}}}$ | $Z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}}$ |

Confidence Interval Critical Values of Z

| Confidence | Z _c | Confidence | Z _c |
|------------|----------------|------------|----------------|
| 90% | 1.645 | 98% | 2.33 |
| 95% | 1.96 | 99% | 2.576 or 2.58 |

Regression line equation $y = ax + b$, a= slope of the line, b = the y-intercept, residual= $y - \hat{y}$;
r= correlation coefficient ($-1 \leq r \leq 1$), r^2 = coefficient of determination

Binomial Distribution: $\mu = np$; $\sigma = \sqrt{np(1-p)}$;

Discrete Probability Distribution: $\mu = \Sigma[X \cdot P(X)]$; $\sigma = \sqrt{\Sigma[(x-\mu)^2 \cdot p(x)]}$

Probability: $nCr = \frac{n!}{r!(n-r)!}$; $nPr = \frac{n!}{(n-r)!}$; $P(A \cup B) = P(A) + P(B) - P(A \cap B)$; $P(A|B) = \frac{P(A \cap B)}{P(B)}$;
 $P(A) + P(A^c) = 1$

Texas Instruments Calculator Shortcuts and Formulas

Descriptive Statistics: (Mean, Standard Deviation, Minimum, Q1, Median, Maximum):

- insert data in calculator STAT → Edit
- Then: STAT → CALC → 1: 1-Vars Stat
- To clear a list: STAT → Edit → go up to the list name (L1, L2, L3...) → CLEAR → Enter
- Restore missing list name: STAT → Edit → go up → 2nd Del → type the name → enter

Linear Regression:

- Correlation coefficient (one-time set up): 2nd 0 → DiagnosticOn → Enter → Enter
- Insert values of X into List1 and values of Y into List2 → STAT → Edit
- Then: STAT → CALC → 4: LinReg(ax + b) → 2nd → 1 → comma → 2nd → 2 → enter
- Or: STAT → CALC → 8: linReg (a + bx) → 2nd → comma → 2nd → 2 → enter

Intervals:

- Stat → TESTS → 1: Z-Test
- Stat → TESTS → 2: T-Test
- STAT → TESTS → 4: 2-SampT-Test
- STAT → TESTS → 5: 1propZ-Test
- STAT → TESTS → A: 1propZ-Interval

Hypothesis Test:

- STAT → TESTS → 1: Z-test
- STAT → TESTS → 2: T-Test
- STAT → TESTS → 4: 2-SampT-Test
- STAT → TESTS → 5: 1propZ-Test

Distributions:

- 2nd → VARS → 2: normalcdf (left bound, right bound, Mean, Standard Deviation)
- 2nd → VARS → 3: invNorm (area to the left, Mean, Standard Deviation)
- 2nd → VARS → 5: tcdf (left bound, right bound, degrees of freedom)
- 2nd → VARS → 0: binomialpdf(number of trials, probability of success, number of successes)