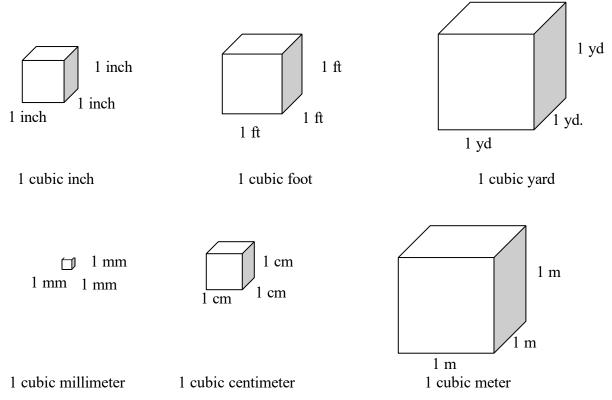


Volume of Basic Geometric Figures

Volume measures the amount of space inside a closed surface. To measure volume we must use a unit of measurement that fills up space. (The linear unit and the square unit will not meet this requirement.)

To measure volume, use cubic units such as:



The abbreviations used for these cubic units are:

cubic inch: in³ cubic foot: ft³ cubic yard: yd³ cubic millimeter: mm³ cubic cm³ cubic m³ centimeter: meter:

FORMULAS: You should memorize the volume formulas for these common geometric solids.



EXPLANATION:

Length × width gives the area of the base, but it also tells the number of cubes that are on the



first layer. If we multiply by the number of layers (the height tells this), we'll have the number of cubic units in the rectangular solid.

$$h = 2$$
 in $U = 4$ in $U = 4$ in

EXAMPLE: Find the volume of a rectangular solid which has a length of 9 inches, a width of 4 inches and a height of 2 inches.

VOLUME = LENGTH × WIDTH × HEIGHT or
$$V = l \cdot w \cdot h$$

= 9in × 4in × 2in
= 72 in³

B. CUBE

The faces of a cube are squares.

$$Volume = Length \times width \times height$$

becomes

$$Volume = side \times side \times side$$

or Volume =
$$(side)^3$$
 or $V = s^3$

EXAMPLE: Find the volume of a cube which is 8 cm on each side.

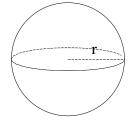
Volume =
$$(\text{side})^3$$

= $(8 \text{ cm})^3$
= 512 cm^3

C. SPHERE

Volume =
$$\frac{4}{3} \cdot \pi \cdot \text{radius} \cdot \text{radius} \cdot \text{radius}$$

or Volume = $\frac{4}{3} \cdot \pi \cdot (\text{radius})^3 = \frac{4}{3} \cdot \pi \cdot r^3$



(There is an explanation for this formula, but it is rather complicated for this lab. Maybe you would accept the challenge to find out <u>why</u> this formula works). You do need to memorize

$$V = \frac{4}{3} \cdot \pi \cdot r^3$$

EXAMPLE: A sphere has a radius of 6 cm. Find its volume. Use $\pi = 3.14$

$$V = \frac{4}{3} \cdot \pi \cdot r^{3}$$

$$= \frac{4}{3} \cdot (3.14) \cdot (6 \text{ cm})^{3}$$

$$= \frac{4}{3} \cdot \frac{3.14}{1} \cdot \frac{26}{1} \cdot \frac{6}{1} \cdot \frac{6}{1}$$

$$= 904.32 \text{ cm}^{3}$$

D. **CYLINDER:** Volume = $\pi \times (\text{radius})^2 \times \text{height}$

This formula will be easier to remember if you see how it compares with the volume formula of a rectangular solid.

CYLINDER

Volume =
$$\pi \times (\text{radius})^2 \times \text{height}$$
 Cylinder:

(Area of base) × height

or $V = \pi \cdot r^2 \cdot h$

base is a circle

EXAMPLE: Find the volume of a cylinder which has a radius of 7 mm and a height of 24 mm. Use $\pi = \frac{22}{7}$

VOLUME =
$$\pi \cdot (\text{radius})^2 \cdot \text{height}$$

= $\frac{22}{7} \cdot \frac{7}{1} \cdot \frac{7}{1} \cdot \frac{24}{1}$
= 3.696 mm³

NOTICE: The units were not used in the work. Volume is always measured in cubit units. Look at the factors. $\frac{22}{7}$ is just a number, but the other three factors have units of "mm."

3



COMPOSITE GEOMETRIC SOLIDS:

To find the volume of composite solids, find the volumes of the solids that you recognize. Then add or subtract these volumes to find the volume of the composite solid. It helps to draw the parts and write your plan!

A cylinder is 14 inches high and has a base with a diameter of 4 inches. A cylindrical column with a diameter of 2 inches is cut out of the center of the larger cylinder. Find the volume of the solid that remains. Use $\pi = \frac{22}{7}$

PLAN: Volume of large cylinder – volume of small cylinder

$$V = \pi \cdot r^{2} \cdot h$$

$$If d = 4 \text{ in, then } r = 2 \text{ in}$$

$$V = \frac{22}{7} \times \frac{2}{1} \times \frac{2}{1} \times \frac{14}{1}$$

$$V = \frac{22}{7} \times 1 \times 1 \times \frac{14}{1}$$

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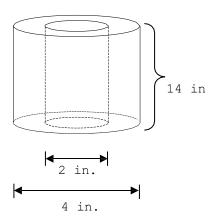
$$V = \frac{22}{7} \times 1 \times 1 \times \frac{14}{1}$$

$$V = \frac{22}{7} \times 1 \times 1 \times \frac{14}{1}$$

$$V = \frac{176 \text{ in}^{3}}{1} \times \frac{14 \text{ in}^{3}}{1}$$

$$V = \frac{14 \text{ in}^{3}}{1}$$

$$V = \frac{14 \text{ in}^{3}}{1}$$



PROBLEMS: You should draw the figure and write the formula first.

1. Find the volume of a cylinder that has a height of 12 ft and a radius of 10 ft. Use $\pi = 3.14$

2. Find the volume of a cube that is 6 inches on each side.

3. Find the volume of a rectangular solid that is 4.6 cm long, 3 cm wide, and 2.8 cm high.



4. Find the volume of a sphere that has a radius of 2 inches. Use $\pi = 3.14$. Round answer to the nearest tenth of a cubic inch.

5. Find the volume of a can that is 8 inches high and has a diameter of 5 inches. Use $\pi = 3.14$.

6. Find the volume of a refrigerator that is 5 ft high, 2½ ft deep and 3 feet wide. (The answer will not give the storage space because much of this is thickness of its walls, etc.)

ANSWER KEY:

- 1. 3768 ft^3
- 2. 216 in^3
- $3. 38.64 \text{ cm}^3$
- 4. 33.5 in³ (rounded)

- 5. 157 in^3
- 6. $37\frac{1}{2}$ ft³

If you use your calculator, you will use 2.5 ft for $2\frac{1}{2}$ ft. The answer will be 37.5 ft³ which is $37\frac{1}{2}$ ft³. Fractions are usually used with U.S.units.

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